

Exercise 1: Chemistry (7 points)**Part 1 and part 2 are independent****Part 1: Study of an aqueous solution of a carboxylic acid**

In a school laboratory, there is a bottle containing a solution (S_0) of a pure carboxylic acid, denoted AH of general formula $C_nH_{2n+1}COOH$ where n is a natural number.

We want to determine the chemical formula of this carboxylic acid and the pK_A of the pair AH/A^- in order to study its reaction with an aqueous solution of sodium methanoate $Na^+_{(aq)} + HCOO^-_{(aq)}$.

Given :

- Molar mass: $M(C)=12g.mol^{-1}$; $M(O)=16g.mol^{-1}$; $M(H)=1g.mol^{-1}$.

1-Determination of the pK_A of the pair AH/A^- and the chemical formula of the acid AH

We prepare a solution (S_A) of the acid AH by dissolving in a distilled water a mass $m = 1,5 g$ of this pure acid. The volume of the solution obtained is $V=500mL$. We take a volume $V_A=20mL$ of the solution (S_A) that we titrate it by an aqueous solution (S_B) of sodium hydroxide $Na^+_{(aq)} + HO^-_{(aq)}$ of molar concentration $C_B = 3,4.10^{-2} mol.L^{-1}$. The pH-metric monitoring allowed obtaining the curve $pH=f(V_B)$ representing the evolution of the pH of the reaction mixture as function of V_B the volume of sodium hydroxide added (Figure 1).

1-1- Write the equation of the reaction of the titration. (0,25pt)

1-2- By using the progress table of the reaction, show that the

expression of the volume V_B is written as : $V_B = \frac{V_{BE} \cdot 10^{pH-pK_A}}{1+10^{pH-pK_A}}$, with V_{BE}

the volume of the sodium hydroxide added at the equivalence point and $0 < V_B < V_{BE}$. (0,75pt)

1-3- Find out the relationship between V_B and V_{BE} so that the relationship $pH = pK_A$ is verified.

Deduce graphically the value of the pK_A . (0,5pt)

1-4- Determine C_A the molar concentration of the solution (S_A). (0,5pt)

1-5- Find out the value of n and deduce the chemical formula of the acid AH studied. (0,75pt)

2- Study of the reaction of the acid AH with méthanoate ions $HCOO^-$.

We mixture a volume $V_1=50mL$ of an aqueous solution of the acid AH of molar concentration

$C=1,0.10^{-2} mol.L^{-1}$ and a volume $V_2=V_1$ of an aqueous solution of sodium methanoate $Na^+_{(aq)} + HCOO^-_{(aq)}$ of same molar concentration C. we model the occurring transformation by the chemical reaction of equation: $AH_{(aq)} + HCOO^-_{(aq)} \rightleftharpoons A^-_{(aq)} + HCOOH_{(aq)}$

Given:

The ion	Na^+	$HCOO^-$	A^-
The molar ionic conductivity ($mS.m^2.mol^{-1}$)	5,01	5,46	3,58

We neglect the contribution of the ions H_3O^+ and HO^- in the conductivity of the solution.

The expression of the conductivity σ of an ionic solution is: $\sigma = \sum_i \lambda_{X_i} \cdot [X_i]$ where $[X_i]$ is the effective molar concentration of the ionic species present in the solution and λ_{X_i} its molar ionic conductivity.

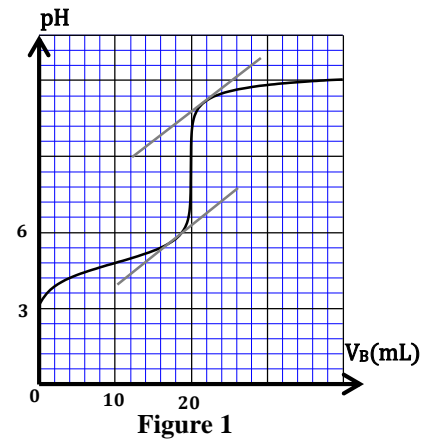


Figure 1

2-1- Show that the expression of the conductivity σ of the reaction mixture at an instant of time t in terms of the progress of the reaction x is written as : $\sigma = 52,35 - 1,88 \cdot 10^4 \cdot x$ with σ expressed in $mS \cdot m^{-1}$ and x in mol. (0,75pt)

2-2- We measure the conductivity of the reaction mixture at the equilibrium state, we find:

$$\sigma_{eq} = 50,092 mS \cdot m^{-1}.$$

2-2-1- Check out that the value of the equilibrium constant K associated to the equation of the reaction is $K \approx 0,1$. (0,5pt)

2-2-2- Deduce the value of the pK_A ' of the pair $HCOOH / HCOO^-$. (0,5pt)

Part 2: study of a nickel – cobalt electrochemical cell

The electric battery is an electrochemical dispositive that produces the electricity by converting a part of the chemical energy to electric energy through the oxidation-reduction reactions.

We consist the nickel – cobalt electrochemical cell, by immersing a blade of nickel in a beaker containing a volume $V = 100 mL$ of an aqueous solution of nickel (II) sulfate: $Ni_{(aq)}^{2+} + SO_{4(aq)}^{2-}$ of initial molar concentration $C_1 = [Ni^{2+}]_i = 10^{-2} mol \cdot L^{-1}$, and a blade of cobalt in another beaker containing a volume $V = 100 mL$ of an aqueous solution of cobalt (II) sulfate: $Co_{(aq)}^{2+} + SO_{4(aq)}^{2-}$ of initial molar concentration $C_2 = [Co^{2+}]_i$. A salt bridge links the two solutions.

We mount in series with this electrochemical cell a resistor, an ammeter and a switch. At an instant $t=0$ we close the circuit. An electric current of intensity I , considered as constant, flows in the circuit.

Given :

- Molar mass of the cobalt: $M(Co) = 58,9 g \cdot mol^{-1}$;
- The faraday Constant: $1F = 9,65 \cdot 10^4 C \cdot mol^{-1}$.
- The equilibrium constant associated to the equation of

the reaction: $Co_{(aq)}^{2+} + Ni_{(s)} \xrightleftharpoons[(2)]{(1)} Ni_{(aq)}^{2+} + Co_{(s)}$ is $Q_{r.e} = K$

at $25^\circ C$.

The curve of figure 2 represents the temporal evolution of the quotient of reaction Q_r .

1- By using the curve $Q_r(t)$, choose the correct

statement, from the following statements: (0,5pt)

- a- The direction of spontaneous evolution of a chemical system consisting the electrochemical cell is the direction (1) of the equation of the reaction.
- b- The electrode of the cobalt is the cathode.
- c- The diagram of the electrochemical cell studied is: $\ominus Ni/Ni^{2+} // Co^{2+}/Co \oplus$.
- d- The conventional direction of the electric current outside the electrochemical cell is from the electrode of nickel to the electrode of cobalt.

2- Determine C_2 . (0,5pt)

3-Find out the expression of the intensity I of the electric current in terms of K , F , C_1 , C_2 , V and t_{eq} , with t_{eq} the instant of time when the equilibrium of the chemical system is reached.

Check out that $I \approx 0,1A$. (0,75pt)

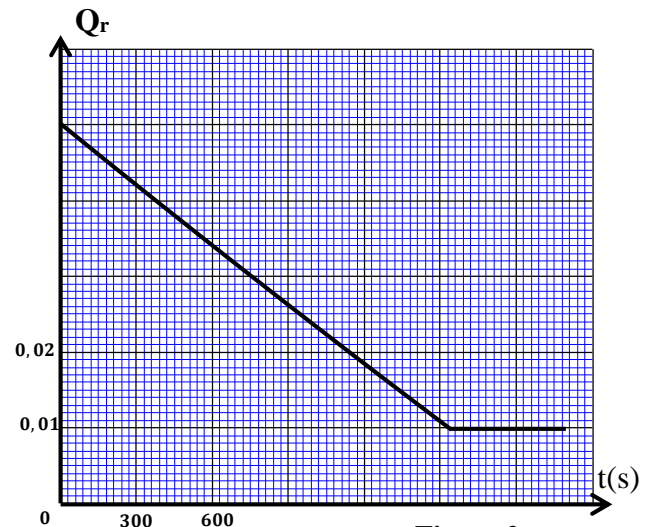


Figure 2

4-Compute Δm the variation of the mass of the electrode of cobalt between the instants $t=0$ and $t = t_{eq}$. (0,75pt)

Exercise 2 : Waves + Nuclear transformations (4points)

Part 1: Study of the diffraction of the light.

The phenomenon of diffraction allows highlighting the wave aspect of the light.

A source of laser producing a monochromatic light of wavelength $\lambda = 750\text{nm}$ lights up a circular diaphragm of an adjusted diameter d . We observe, on the screen placed at the distance D from the diaphragm, a circular light spot of a diameter L surrounded by a dark and light alternatives rings. (Figure 1) We vary d , and we denote the value of corresponding L .

The curve of figure 2 represents the curve $L = f\left(\frac{1}{d}\right)$.

Given :

- The distance diaphragm-screen: $D = 1,50\text{ m}$
- The law associated of the diffraction with the circular diaphragm has the expression: $\theta = \frac{\alpha \cdot \lambda}{d}$ with θ the angular deviation expressed in radian and α a coefficient of correction linked to the circular shape of the slit.

1- Show in the case of small angular deviations, where

$$\tan(\theta) \approx \theta(\text{rad}) \text{ that: } L = \frac{2\alpha \cdot \lambda \cdot D}{d}. \quad (0,5\text{pt})$$

2-Verify that $\alpha = 1,22$. (0,5pt)

3- We replace the diaphragm with an opaque plate pierced with a hole of an unknown diameter d' , the diameter of the central spot obtained is : $L'=1,5\text{cm}$.

3-1- Determine d' . (0.5pts)

3-2- We replace the source of laser with a source of white light, we observe on the screen, a central iridescent spot consisted with a white central part of diameter L_B . Knowing that the wavelength λ of visible spectrum in the vacuum is $\lambda_1=0,4\mu\text{m} < \lambda < \lambda_2=0,8\mu\text{m}$.

3-2-1- Indicate between λ_1 and λ_2 , the wavelength corresponding to the red radiation. (0,25pt)

3-2-2- Determine L_B . (0,75pt)

Part 2: The radioactivity of the polonium.

The nucleus of polonium ${}^{210}_{84}\text{Po}$ spontaneously decays into a nucleus of lead ${}^{206}_{82}\text{Pb}$ with emission of a particle α .

In this part, we propose to study the energy balance of this transformation and the evolution during time of this transformation.

On the diagram of figure 1 are placed the values of the mass of the following systems: (the nucleus of polonium 210); (separated nucleons); (the nucleus of lead 206 + α).

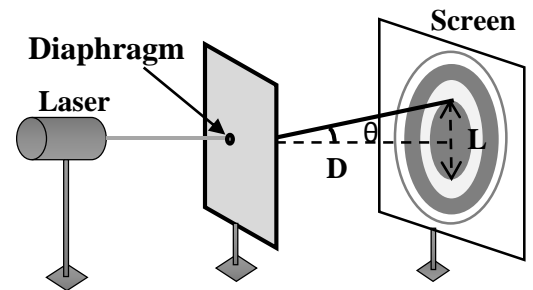


Figure 1

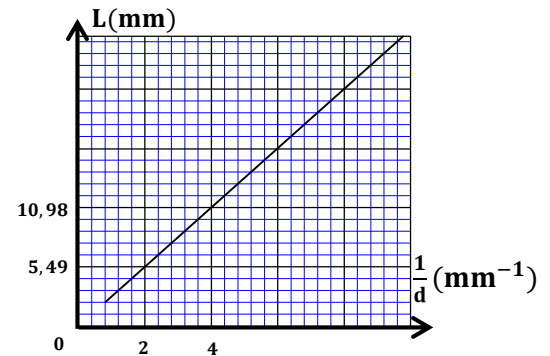


Figure 2

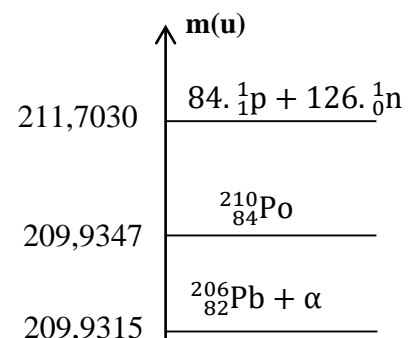


Figure 1

Given :

- The molar mass of polonium 210 : $M=210\text{g}\cdot\text{mol}^{-1}$;
- Atomic mass unit: $1\text{u}=931,5\text{MeV}\cdot\text{c}^{-2}$.
- Avogadro constant: $N_A=6,02\cdot 10^{23}\text{mol}^{-1}$.

1- Choose the correct statement from the following statements : (0,25pt)

- a- The α - decay corresponds to the emission of a neutron.
- b- The α - decay concerns light nuclei.
- c- The half-life $t_{1/2}$ of a sample is the duration after which 63% of the sample disintegrated.
- d- The binding energy per nucleon of lead 206 is greater than that of polonium 210.

2- By exploiting the diagram of figure 1:

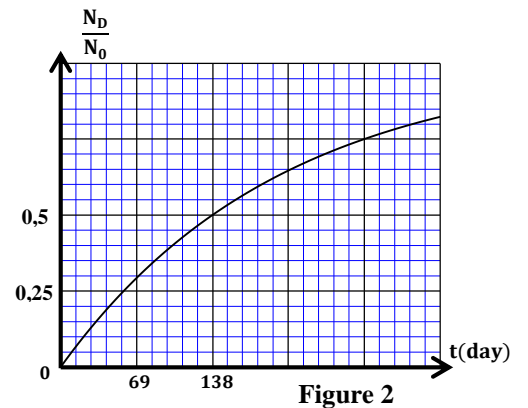
2-1- Compute, in MeV/nucleon , the binding energy per nucleon of the nucleus ${}_{84}^{210}\text{Po}$. (0,25pt)

2-2- Compute, in MeV , the energy $|\Delta E|$ released by the disintegration of a mass $m=1\text{mg}$ of polonium 210. (0,25pt)

3- We denote by N_D the number of nuclei of polonium disintegrated at an instant t and N_0 the number of nuclei of polonium 210 contained in the sample at $t=0$. The curve of figure 2 represents the variations of $\frac{N_D}{N_0}$ as function of time.

3-1- By exploiting the curve of figure 2, determine in day The half-life $t_{1/2}$ of the polonium 210. (0,25pt)

3-2- Let t_1 the instant at which we have: $\frac{N_D}{N} = 3$, with N the number of nuclei of the polonium remaining at the same instant. Find out in day the value of t_1 . (0,5pt)



Exercise 3 : Electricity (4 points)

Part 1 and part 2 are independent

This exercise aims to study:

- The response of the RC dipole to a step of voltage.
- Forced oscillations in RLC series circuit.

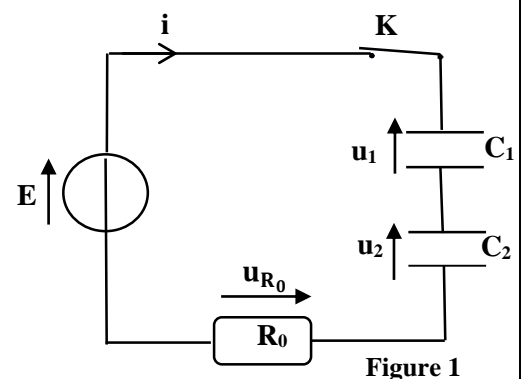
Part1: Study of RC dipole

We perform the electric circuit of figure 1 which consists of:

- An ideal generator of voltage of e.m.f E ;
- A resistor of resistance R_0 ;
- Two capacitors (C_1) and (C_2) without initial charge, respectively of capacitances $C_1=5\mu\text{F}$ and $C_2 > C_1$;
- A switch K .

We close the switch K at an instant $t=0$,

1-1- Express u_1 the voltage between terminals of (C_1) in terms of C_1, C_2 and u_2 the voltage between terminals of (C_2) . (0,25pt)



1-2- Show that the differential equation verified by u_2 is written as : $u_2 + \frac{R_0 \cdot C_1 \cdot C_2}{C_1 + C_2} \cdot \frac{du_2}{dt} = \frac{C_1 \cdot E}{C_1 + C_2}$. (0,5pt)

1-3- Knowing that solution of differential equation is written as: $u_2(t) = A(1 - e^{-\alpha t})$

Find out the expression of the constant A and that of α in terms of the parameters of the circuit. (0,5pt)

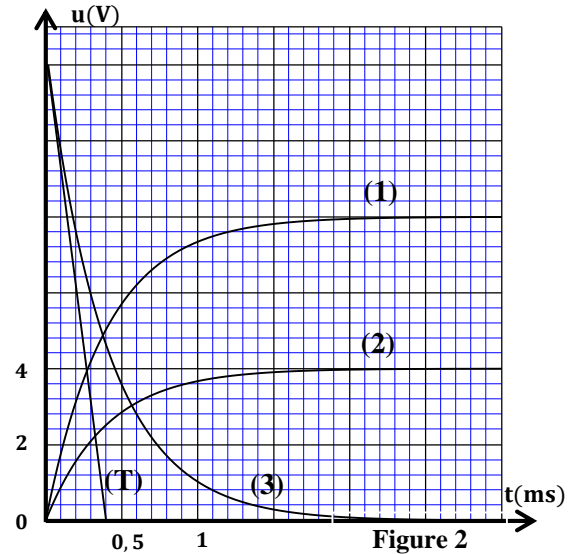
2- The curves of figure 2 represent the evolution during the time of voltages u_1 , u_2 and u_{R_0} the voltage between terminals of the resistor.

(T) represents the tangent of the curve 3 at the point of abscise $t = 0$.

2-1- Associate the voltage $u_2(t)$ with the corresponding curve. (0,25pt)

2-2- Determine the value of C_2 and that of R_0 . (0,5pt)

2-3- Calculate Ee the total electric energy stored in both capacitors when the steady state is established. (0,25pt)



Part 2: Study of forced oscillations in RLC series circuit

We perform the electric circuit of figure 3, which consists:

- A low frequency generator (GBF), which delivers a sinusoidal alternating voltage of a constant frequency N and a constant maximal voltage U_m ;
- A capacitor of capacitance $C_0 = 10 \mu\text{F}$;
- An inductor (b) of inductance $L = 86 \text{mH}$ and of resistance r ;
- A resistor of resistance $R = 20 \Omega$.

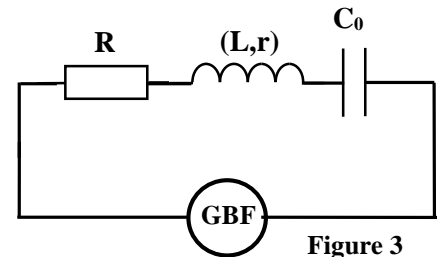


Figure 3

The generator applies a voltage $u(t) = U_m \cdot \cos(2\pi \cdot N \cdot t + \varphi)$, an electric current of intensity $i(t) = I_m \cdot \cos(2\pi \cdot N \cdot t)$ flows in the circuit.

We visualize, with the help of an adequate computing system, the voltage $u_R(t)$ between the terminals of the resistor and the voltage $u(t)$ between the terminals of the generator.

We obtain the oscillogram represented in figure 4.

1- Determine the value of φ and that of the impedance Z of the circuit. (0,5pt)

2- Compute the average power P dissipated by Joule effect in the circuit and deduce the value of r . (0,5pt)

3- To obtain the electric resonance, we mount a capacitor of capacitance C with capacitor of the capacitance C_0 .

3-1- Determine the value of C . We take $\pi^2 = 10$. (0,5pt)

3-2- Compute the intensity of the effective current in the circuit. (0,25pt)

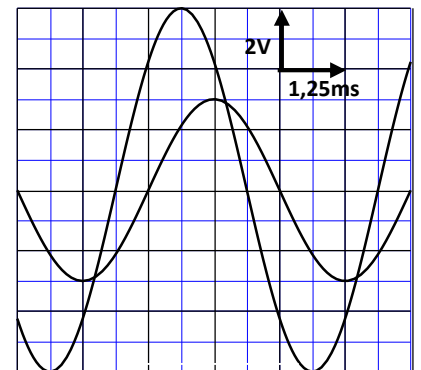


Figure 4

Exercise 4 : Mechanics (5 points)**Part 1 and part 2 are independent****Part 1: Motion of mechanical system**

We consider a pulley (P) of radius $r = 5\text{cm}$ susceptible to rotate in a vertical plane around an horizontal fixed axis (Δ) passing through its center I and whose the moment of inertia about this axis is J_{Δ} .

We wrap an inextensible wire of negligible mass around the pulley (P), on the other end of the wire is attached a solid (S) of mass $m = 100\text{g}$ and of center of inertia G. During the motion, the wire does not slip on the pulley (figure1).

We consider a point M on the circumference of the pulley.

The point M initially starts from the position M_0 belonging on the vertical line passing through point I and the center of inertia G of the solid (S) starts from a position of coordinate $z=0$ in the frame of reference (O, \vec{k}) .

We locate, at any instant of time, the position of the center of inertia G by the z coordinate and the position of the point M by the angular displacement

$$\theta = (\overrightarrow{IM}_0, \overrightarrow{IM}).$$

We take the gravitational field strength $g=10\text{m.s}^{-2}$

1- We neglect all frictions. The curve of figure (2) represents the evolution of the angular velocity $\dot{\theta}$ of the pulley as function of time.

1-1- Determine, by justifying your answer, the nature of motion of the pulley (P) and calculate its angular acceleration $\ddot{\theta}$. (0,5 pt)

1-2- At the instant $t_1 = 3\text{s}$, compute the value of the tangential acceleration a_t and that of normal acceleration a_n of the motion of M. (0,5 pt)

1-3- By using a dynamic study, show that $J_{\Delta} = 10^{-3}\text{kg.m}^2$. (0,5 pt)

2- At the instant $t_1 = 3\text{s}$ the wire is cut and the solid (S) continues its fall.

We consider that the frictional fluids force applied by air is written

as: $\vec{f} = -\mu.v^2\vec{k}$ with μ is the coefficient of friction and v the velocity of G.

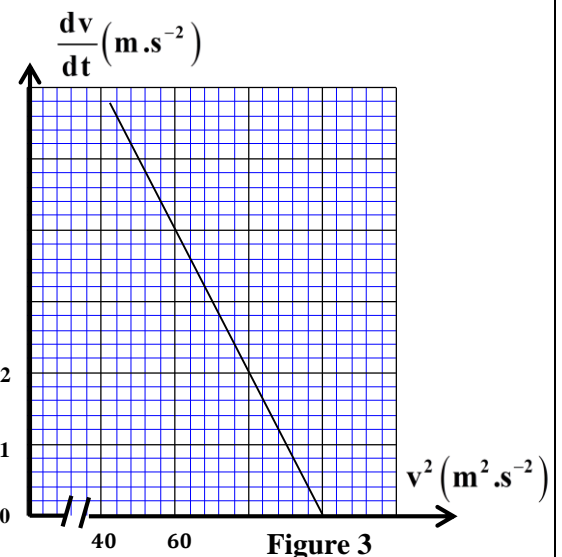
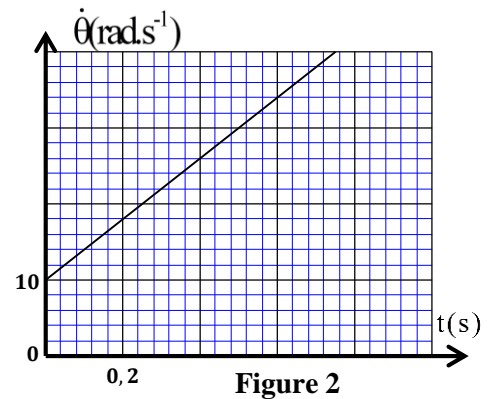
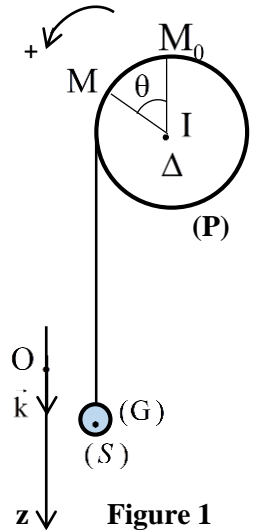
We neglect the Archimedes' force in front of other forces.

2-1- Compute the velocity of (S) at the instant $t_1 = 3\text{s}$. (0,25 pt)

2-2- Establish the differential equation verified by the velocity v when $t \geq t_1$ (0,25 pt)

2-3- The curve of figure 3 represents the variations of $\frac{dv}{dt}$ as function of v^2 .

Determine the value of the terminal velocity V_L of the solid (S), and that of the coefficient μ . (0,5pt)



Part 2 : Motion of an elastic pendulum.

The elastic pendulum is a mechanical system performing an oscillating motion around its rest position.

This part aims to determine some quantities of this oscillator.

The pendulum studied consists of a solid (S), of center of inertia

G and of mass $m = 100\text{g}$, which is attached to the end of a spring

with non-contiguous turns, of a negligible mass and spring constant K. We fix the other end of the spring to a fixed stand.

The solid (S) slides without friction on the inclined plane at an angle $\alpha = 30^\circ$ to the horizontal plane.

We study the motion of the center of inertia G of the solid in

frame of reference $R(O, \vec{i}, \vec{j})$ linked to the earth assumed

Galilean.

We locate the position of G at an instant t by the displacement x on the x-axis (O, \vec{i}).

At the rest position, the displacement x of G is zero in the frame of reference (figure 4).

Given:

- The intensity of the gravitational acceleration: $g = 10\text{m.s}^{-2}$;

- We take $\pi^2 \approx 10$

1- Show that the expression of the extension Δl_0 of the spring at the rest position is written as :

$$\Delta l_0 = -\frac{mg \cdot \sin(\alpha)}{K}. \quad (0,25\text{pt})$$

2- We displace (S) from its rest position, and we release it at an instant of date $t = 0$ with an initial velocity $\vec{V}_0 = V_0 \vec{i}$.

The curve of figure 5 represents the evolution during time of the component v_x of the velocity vector of G.

2-1- Applying the Newton's second law, Establish the differential equation of the motion verified by the displacement x of G. (0,5pt)

2-2- The solution of the differential equation is written as:

$$x(t) = X_m \cdot \cos\left(\frac{2\pi}{T_0} t + \varphi\right), \text{ with } T_0 \text{ the natural period of the oscillator.}$$

Find out the value of X_m , of φ and that of K. (0,75pt)

2-3- Deduce the vectorial expression of the resultant of the forces applied to (S) as function of time. (0,25pt)

2-4- We choose as reference level the elastic potential energy ($E_{pe} = 0$) when the spring is not deformed and as reference level of the gravitational potential energy ($E_{pp} = 0$) the horizontal plan passes through G at the rest position.

2-4-1- Show that the expression of the mechanical energy of the oscillating system is written as:

$$E_m = \frac{1}{2} m \dot{x}^2 + \frac{1}{2} K(x^2 + \Delta l_0^2). \quad (0,5\text{pt})$$

2-4-2- Compute the value of E_m . (0,25pt)

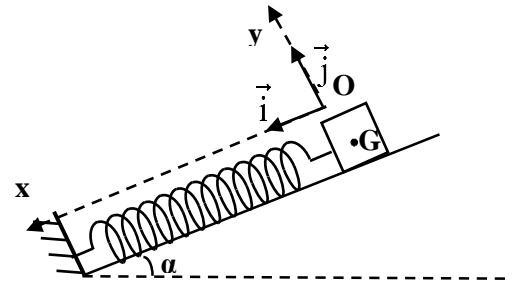


Figure 4

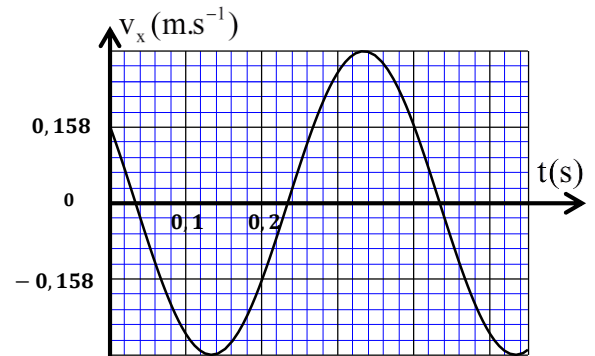


Figure 5

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المسالك الدولية
الدورة العادية 2024

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عناصر الإجابة

NR 30E

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مدة الإنجاز

الفيزياء والكيمياء

المادة

7

المعامل

شعبة العلوم الرياضية (أ) و (ب) (خيار إنجليزية)

الشعبة أو المسلك

Exercise 1 : Chemistry (7 points)

	Question	Answers	Marking scale	Question reference in the framework
Part 1	1-1	Equation of titration reaction with one arrow	0,25	Write the equation of titration reaction (use only one arrow) . -Define the final progress rate of a reaction, and determine it using experimental data. -Determine and exploit the point of equivalence. -Write and use the expression of the acid dissociation constant K_A associated with the reaction of an acid with water. - Justify the choice of a suitable indicator to determine the equivalence. - Give and use the expression of the reaction quotient Q_r through the reaction equation. . --Know that the ionic product of water K_w , is the equilibrium constant associated with the equation of the reaction of water autoprotolysis (self-ionization of water). -Determine the nature of aqueous solution (acid, basic or neutral) based on its pH value. -Determine the pH for an aqueous solution.
	1-2	Demonstration	0,75	
	1-3	$V_B = \frac{V_{Be}}{2}$ $pK_A = 4,8$	0,25 0,25	
	1-4	$C_A = 3,4.10^{-2} \text{ mol.L}^{-1}$	0,5	
	1-5	$n = 3$ C_3H_7COOH	0,5 0,25	
	2-1	Demonstration	0,75	
	2-2-1	Verification	0,5	
	2-2-2	$pK'_A = 3,8$	0,5	
	Part 2	1	-d-	
2		Method $C_2 = 0,2 \text{ mol.L}^{-1}$	0,25 0,25	
3		$I = \frac{2F.V.(C_1 - K.C_2)}{(1 + K).t_{eq}}$; $I \approx 0,1A$	0,5 0,25	
4		$\Delta m \approx -46,7 \text{ mg}$	0,75	

Exercise 2 : waves + Nuclear transformations (4 points)

	Question	Answers	Marking scale	Question reference in the framework
Part 1	1	Demonstration	0,5	<ul style="list-style-type: none"> - Know that light has a wave aspect, based on the diffraction phenomenon. - Know the influence of the size of the slit (opening) or of the obstacle on the diffraction phenomenon - Exploit a document or a diffraction pattern in the case of light waves. - Know (Recall) and exploit the relationship: $\lambda = c / \nu$. - Know the boundaries of wavelengths and their colours for the visible spectrum in the vacuum. - Know the frequency of a monochromatic radiation does not change as it passes from one transparent medium to another. - Know that the transparent media are more or less dispersive. - Know (Recall) and exploit the relationship $n = \frac{c}{v}$.
	2	Verification	0,5	
	3-1-	Method $d' = 1,83 \cdot 10^{-4} \text{m}$	0,25 0,25	
	3-2-1	$\lambda_2 = 0,8 \mu\text{m}$	0,25	
	3-2-2	Method $L_B = 8 \cdot 10^{-3} \text{m}$	0,5 0,25	
Part 2	1	d	0,25	<ul style="list-style-type: none"> - Define a radioactive nucleus - Know and exploit the two laws of conservation. - Define the radioactivity α, β^+, β^- and the γ-radiation . - Write the equation of a nuclear reaction by applying the two conservation laws. - Recognise the type of radioactivity using the equation of a nuclear reaction. - Know and exploit the law of the radioactive decay, and exploit its curve. - Know that 1Bq is equal to one decay per second. - Define the time constant τ and the half-life $t_{1/2}$. - Exploit the relationships between τ, λ and $t_{1/2}$. - Define and calculate the mass defect and the binding energy. - Define and calculate the binding energy per nucleon and exploit it. - Use different units of mass, energy and the relationships between their units. - Exploit the binding energy per nucleon curve (Aston curve) to identify the most stable nucleus. - Know the relationship of the mass-energy equivalence; and calculate the energy of mass.
	2-1	7,83MeV/nucleon	0,25	
	2-2	$ \Delta E = 8,54 \cdot 10^{18} \text{MeV}$	0,25	
	3-1	$t_{1/2} = 138 \text{jour}$	0,25	
	3-2	$t_1 = 276 \text{jour}$	0,5	

Exercise 3 : Electricity (4 points)

	Question	Answers	Marking scale	Question reference in the framework
Part 1	1-1	$u_1 = \frac{C_2}{C_1} \cdot u_2$	0,25	- Know and exploit the relationship $i = \frac{dq}{dt}$ for a capacitor in receiver convention.
	1-2	Demonstration	0,5	- Know and exploit the relationship $q = C \cdot u$.
	1-3	$A = \frac{C_1 \cdot E}{C_1 + C_2}$, $\alpha = \frac{C_1 + C_2}{R_0 \cdot C_1 \cdot C_2}$	0,25	- Know the capacitance of a capacitor, its unit F et ses sous multiples and their submultiples $\mu F, nF$ et pF .
			0,25	- Determine the capacitance of a capacitor graphically or by calculation.
	2-1	(2) corresponds to u_2	0,25	- Know the capacitance of the equivalent capacitor in series or in parallel assemblies; and recall the interest of each one.
	2-2	$C_2 = 10\mu F$; $R_0 = 120\Omega$	0,25	- Find out the differential equation and verify its solution when the RC dipole is submitted to a step voltage.
			0,25	- Determine the voltage expression $u_C(t)$ between capacitor terminals when the RC dipole is submitted to a step voltage, and deduce both the expression of the intensity current in the circuit and the capacitor charge
2-3	$Ee = 2,4 \cdot 10^{-4} J$	0,25		
Part 2	1	$\varphi = \frac{\pi}{4}$ $Z = 40\Omega$	0,25	Know the role of the driver and the resonating system.
			0,25	- Know and exploit the expression $ \varphi = \frac{2 \cdot \pi \cdot \tau}{T}$ of the phase of physical quantity relative to another.
	2	$P = 0,318W$ $r = 8,26\Omega$	0,25	- Know and exploit the impedance expression $Z = \frac{U}{I}$ of a circuit.
			0,25	- Know the unit of the impedance (Ω) .
3-1	method $C \approx 26,6\mu F$	0,25	- Recognise the electric resonance phenomenon and its characteristics.	
		0,25	- Know the instantaneous power in the alternating sinusoidal state.	
3-2	$I = 0,15A$	0,25	- Find out and exploit the average power expression $P = U \cdot I \cdot \cos\varphi$	
				- Know the power factor.

Exercise 4 : Mechanics (5 points)

	Question	Answers	Marking scale	Question reference in the framework
Part 1	1-1	M.R.U.V ; $\ddot{\theta} = 40\text{rad.s}^{-2}$	0,25 0,25	<ul style="list-style-type: none"> - Know the angular acceleration expression and its unit. - Know and exploit the expressions of the two components a_n and a_t in terms of angular quantities. - Know and apply the fundamental relationship of dynamics in the case of rotation around a fixed axis in order to establish the differential equation of the motion, and solve it. - Know the unit of the moment of inertia. - Know and exploit the characteristics of a uniformly varied rotational motion and its parametric equations . - Apply Newton's second law and the fundamental relationship of dynamics on a mechanical system consisting of two solids, one in straight translational motion and the other in rotational motion, to establish the differential equation and to determine kinetic and dynamic quantities. - Exploit the curve $v=f(t)$ to determine: <ul style="list-style-type: none"> * the terminal speed; * the characteristic time τ ; * the initial state and the steady state. . - Apply Newton's second law to find out the differential equation of a solid's centre of inertia motion in frictional vertical fall. - Know and apply the Euler's method to solve approximately differential equation
	1-2	$a_t = 2\text{m.s}^{-2}$ $a_n = 845\text{m.s}^{-2}$	0,25 0,25	
	1-3	Demonstration	0,5	
	2-1	$v(t_1) = 6,5\text{m.s}^{-1}$	0,25	
	2-2	Method	0,25	
	2-3	$V_L = 10\text{m.s}^{-1}$ $\mu = 10^{-2}(\text{S.I})$	0,25 0,25	
Part 2	1	Demonstration	0,25	<ul style="list-style-type: none"> -Know the characteristics of the restoring force exerted by a spring on a solid in motion. -Exploit the curves: $x_G(t)$, $v_G(t)$ and $a_G(t)$. -Apply Newton's second law to the oscillating system (solid-spring) to establish the differential equation of motion and verify its solution when the oscillating system vibrates in the following situations: horizontal, inclined or vertical. - Determine the type of motion of the oscillating system (solid-spring); write the equations: $x_G(t)$, \dot{x} and \ddot{x} and exploit them. Know the meaning of the physical quantities involved in the expression of the parametric equation of the oscillating system (solid-spring) and determine them using the initial conditions. Establish the expression of the natural period of the oscillating system (solid-spring). Know and exploit both the expression of the natural period and that of the natural frequency of the oscillating system (solid-spring). . Know and exploit the expression of the elastic potential energy. Know and exploit the expression of the mechanical energy of a solid-spring system . -Exploit the conservation and the non-conservation of the mechanical energy of a solid-spring system .
	2-1	$\ddot{x} + \frac{K}{m}x = 0$	0,5	
	2-2	$X_m = 2\text{cm}$	0,25	
		$\varphi = -\frac{\pi}{6}$	0,25	
		$K = 25\text{N.m}^{-1}$	0,25	
	2-3	$\sum \vec{F}_{\text{ext}} = -0,5\cos(5\pi t - \frac{\pi}{6}) \cdot \vec{i}$	0,25	
2-4-1	Demonstration	0,5		
2-4-2	$E_m = 10\text{mJ}$	0,25		