

**الامتحان الوطني الموحد للبكالوريا
المسالك الدولية – خيار إنجليزية
الدورة العادية 2019
– الموضوع –**

٢٠١٩ | ملخص
٢٠١٩ | ملخص
٢٠١٩ | ملخص
٢٠١٩ | ملخص
٢٠١٩ | ملخص



السلطة المغربية
وزارة التربية والتكوين
والتكوين المهني
والتعليم العالي والبحث العلمي

المركز الوطني للتقويم والامتحانات والتوجيه

***** NS22E *****

NS22E

3	مدة الاجاز	الرياضيات	المادة
7	المعامل	مسلك علوم الحياة والأرض ومسلك العلوم الفيزيائية – خيار إنجليزية	الشعبة أو المسلك

GENERAL INSTRUCTIONS

- ✓ The use of non-programmable calculator is allowed ;
- ✓ The exercises can be treated in the preferred order by the candidate ;
- ✓ The use of red color when writing solutions is to be avoided.

COMPONENTS OF THE EXAM

- ✓ The exam consists of three exercises and a problem , independent of each other according to the fields as follows :

Exercise 1	Geometry in space	3 points
Exercise 2	Complex numbers	3 points
Exercise 3	Calculating probabilities	3 points
Problem	Study of numerical function, calculating integrals and numerical sequences	11 points

- ✓ \ln denotes the Napierian logarithm function

Exercise 1 : (3 points)

In the space referred to an orthonormal direct coordinate system $(O, \vec{i}, \vec{j}, \vec{k})$, we consider the points $A(1, -1, -1)$, $B(0, -2, 1)$ and $C(1, -2, 0)$

0.75 1)a) Show that $\overrightarrow{AB} \wedge \overrightarrow{AC} = \vec{i} + \vec{j} + \vec{k}$

0.5 b) Deduce that $x + y + z + 1 = 0$ is a cartesian equation of the plane (ABC)

0.75 2) Let (S) the sphere of equation $x^2 + y^2 + z^2 - 4x + 2y - 2z + 1 = 0$

Show that the center of the sphere (S) is the point $\Omega(2, -1, 1)$ and that its radius is $R = \sqrt{5}$

0.5 3)a) Calculate $d(\Omega, (ABC))$ the distance of the point Ω to the plane (ABC)

0.5 b) Deduce that the plane (ABC) intersects the sphere (S) along a circle (Γ)

(the determination of the center and radius of the circle (Γ) is not required)

Exercise 2 : (3 points)

0.75 1) Solve in the set of complex numbers \mathbb{C} the equation : $z^2 - 2z + 4 = 0$

2) In the complex plane referred to an orthonormal direct coordinate system (O, \vec{u}, \vec{v}) ,

we consider the points A , B , C and D of respective affixes $a = 1 - i\sqrt{3}$, $b = 2 + 2i$,
 $c = \sqrt{3} + i$ and $d = -2 + 2\sqrt{3}$

0.5 a) Verify that $a - d = -\sqrt{3}(c - d)$

0.25 b) Deduce that the points A , C and D are collinear

0.5 3) Let z be the affix of a point M in the complex plane and z' the affix of the point M' image of M
by the rotation R with center O and angle $-\frac{\pi}{3}$

Verify that $z' = \frac{1}{2}az$

4) Let the point H the image of the point B by the rotation R , and h its affix, and P the point of affix p such that $p = a - c$

0.5 a) Verify that $h = ip$

0.5 b) Show that the triangle OHP is rectangle and isosceles in O .

Exercise 3 : (3 points)

An urn contains ten balls : three green balls, six red balls and one black ball. All the balls are indistinguishable to the touch .

We draw randomly and simultaneously three balls from the urn.

We consider the following events: A : "Get three green balls"
 B : "Get three balls of the same color"
 C : "Get at least two balls of the same color"

2) Show that $p(A) = \frac{1}{120}$ and $p(B) = \frac{7}{40}$

1) Calculate $p(C)$

Problem : (11 points)

First part

We consider the numerical function f defined on $]0, +\infty[$ by $f(x) = x + \frac{1}{2} - \ln x + \frac{1}{2}(\ln x)^2$

and (C) the curve of f in an orthonormal coordinate system (O, \vec{i}, \vec{j}) (unit: 1 cm)

0.5) 1) Calculate $\lim_{\substack{x \rightarrow 0 \\ x > 0}} f(x)$ and then interpret geometrically the obtained result

0.25) 2)a) Verify that for every x on $]0, +\infty[$, $f(x) = x + \frac{1}{2} + \left(\frac{1}{2} \ln x - 1 \right) \ln x$

0.5) b) Deduce that $\lim_{x \rightarrow +\infty} f(x) = +\infty$

0.5) c) Show that for every x on $]0, +\infty[$, $\frac{(\ln x)^2}{x} = 4 \left(\frac{\ln \sqrt{x}}{\sqrt{x}} \right)^2$

and then deduce that $\lim_{x \rightarrow +\infty} \frac{(\ln x)^2}{x} = 0$

0.75) d) Show that the curve (C) admits a parabolic branch in the direction of the line (Δ)
 which an equation is $y = x$ at $+\infty$

0.5) 3)a) Show that for every x on $]0, 1]$: $(x-1) + \ln x \leq 0$

and for every x on $[1, +\infty[$: $(x-1) + \ln x \geq 0$

1) b) Show that for every x on $]0, +\infty[$, $f'(x) = \frac{x-1+\ln x}{x}$

0.5) c) Set up the table of variations of the function f

0.5) 4)a) Show that $f''(x) = \frac{2-\ln x}{x^2}$ for every x on $]0, +\infty[$

0.5) b) Deduce that the curve (C) admits an inflection point which coordinates will be determined

0.5 5) a) Show that for every x on $]0, +\infty[$, $f(x) - x = \frac{1}{2}(\ln x - 1)^2$,

and then deduce the relative position of the line (Δ) and the curve (C)

1 b) Sketch the line (Δ) and the curve (C) in the same system coordinate (O, \vec{i}, \vec{j})

0.5 6) a) Show that the function $H : x \mapsto x \ln x - x$ is a primitive of the function $h : x \mapsto \ln x$ on $]0, +\infty[$

0.75 b) Using an integration by parts, show that $\int_1^e (\ln x)^2 dx = e - 2$

0.5 c) Calculate, in cm^2 , the area enclosed between the curve (C) , the line (Δ) , and the lines
of equations $x=1$ and $x=e$

Second part :

Let (u_n) be the numerical sequence defined by $u_0 = 1$ and $u_{n+1} = f(u_n)$ for every natural number n

0.5 1) a) Show by induction that $1 \leq u_n \leq e$ for every natural number n

0.5 b) Show that the sequence (u_n) is increasing

0.5 c) Deduce that the sequence (u_n) is convergent.

0.75 2) Calculate the limit of the numerical sequence (u_n) .

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- عناصر الإجابة -

٢٠١٩-٢٠٢٠م
٢٠٢١-٢٠٢٢م
٢٠٢٣-٢٠٢٤م
٢٠٢٥-٢٠٢٦م



السلطة الوطنية
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NR22E

المادة	الشعبة أو المسار	الرياضيات	مدة الاجاز	3
مسار علوم الحياة والأرض ومسار العلوم الفيزيائية - خيار إنجليزية	العلوم الفيزيائية	الرياضيات	المعامل	7

On prendra en compte les différentes étapes de la solution et on acceptera toute méthode correcte .

Exercice1 (3points)

1	a	0.75
	b	0.5
2	0.75 : 0.5 pour le centre et 0.25 pour le rayon	
3	a	0.5
	b	0.5

Exercice2 (3points)

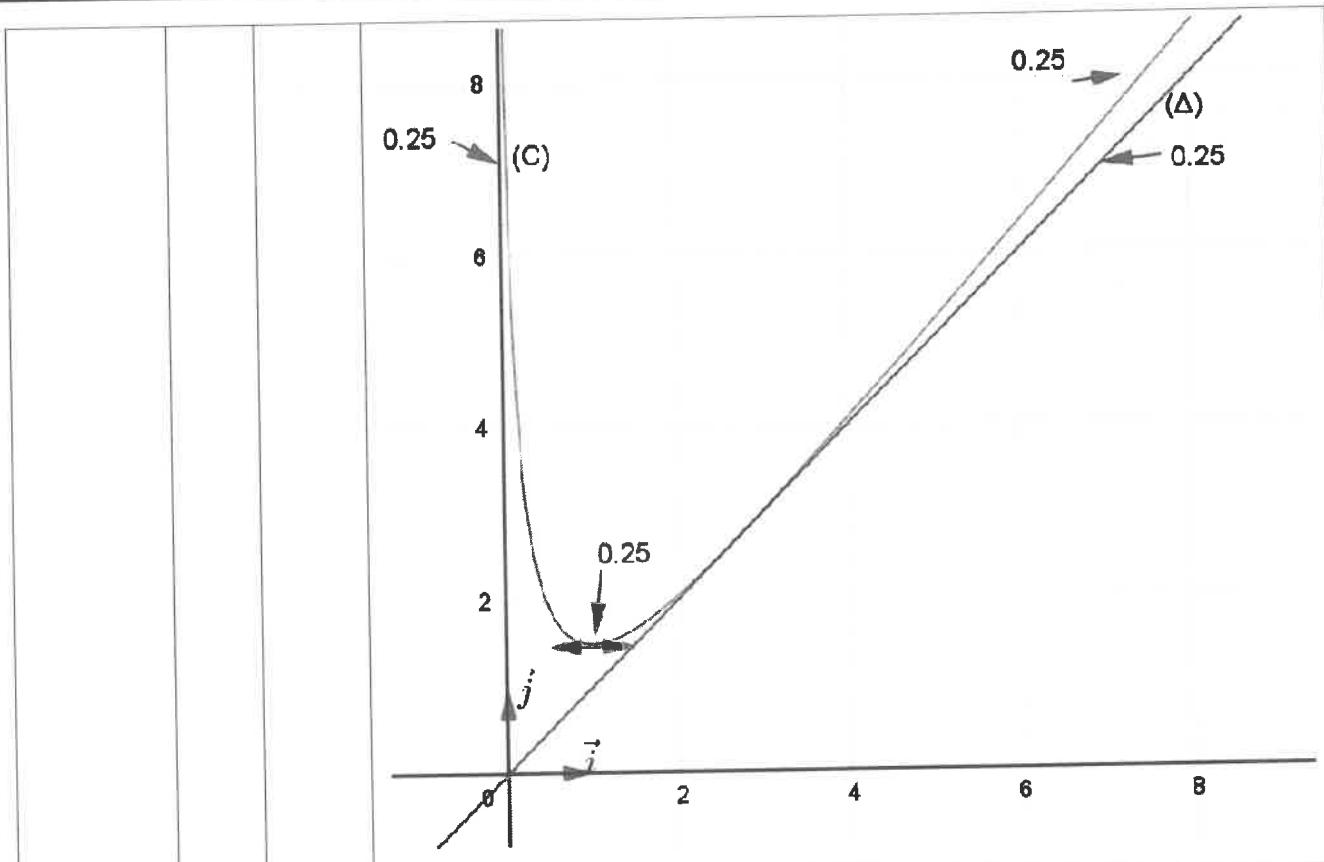
1	0.75 : 0.25 pour le discriminant et 0.25 pour chacune des solutions	
2	a	0.5
	b	0.25
3	0.5	
4	a	0.5
	b	0.5 : 0.25 pour le triangle rectangle et 0.25 pour le triangle isocèle

Exercice3 (3points)

1	$2 : 1 \text{ pour } p(A) = \frac{1}{120} \text{ et } 1 \text{ pour } p(B) = \frac{7}{40}$
2	$1 \text{ pour } p(C) = \frac{17}{20}$

Problème (11 points)

	1	0.5 : 0.25 pour le calcul de la limite et 0.25 pour l'interprétation
Première partie	a	0.25
	b	0.5
	c	0.5 : 0.25 pour l'égalité et 0.25 pour la déduction de la limite
	d	0.75 : 0.25 pour la limite $\lim_{x \rightarrow +\infty} \frac{f(x)}{x}$, 0.25 pour la limite $\lim_{x \rightarrow +\infty} (f(x) - x)$ et 0.25 pour la direction asymptotique
3	a	0.5 : 0.25 pour chaque inégalité
	b	1
	c	0.5
4	a	0.5
	b	0.5
5	a	0.5 : 0.25 pour l'égalité et 0.25 pour la déduction
	b	1 point à distribuer selon ce qui est précisé sur la figure ci-dessous



		a	0.5
6		b	0. 75 : 0.25 pour la technique de l'intégration par parties et 0.5 pour le calcul de l'intégrale
		c	0. 5 : 0.25 pour la formule de l'aire et 0.25 pour le calcul
		a	0.5
Deuxième partie	1	b	0.5
		c	0.5
		2	0.75 : 0.5 pour vérifier les conditions du théorème et 0.25 pour le calcul de la limite