

Exercise 1 (3 points) :

In the space referred to a direct orthonormal coordinate system $(O, \vec{i}, \vec{j}, \vec{k})$ we consider the points $A(0,1,1)$, $B(1,2,0)$ and $C(-1,1,2)$

- 0,5 1) a) Show that $\overrightarrow{AB} \wedge \overrightarrow{AC} = \vec{i} + \vec{k}$
0,25 b) Deduce that $x+z-1=0$ is a cartesian equation of the plane (ABC)
- 0,5 2) Let (S) be the sphere with the center $\Omega(1,1,2)$ and the radius $R = \sqrt{2}$. Determine an equation of the sphere (S)
- 0,5 3) Show that the plane (ABC) is tangent to the sphere (S) at the point A
- 0,25 4) We consider the line (Δ) passing through the point C and perpendicular to the plane (ABC)
a) Determine a parametric equation of the line (Δ)
- 0,5 b) Show that the line (Δ) is tangent to the sphere (S) at a point D whose the coordinates will be determined.
- 0,5 c) Calculate the scalar product $\overrightarrow{AC} \cdot (\vec{i} + \vec{k})$ then deduce the distance $d(A, (\Delta))$.

Exercise 2 (3 points) :

In the complex plane referred to a direct orthonormal coordinate system (O, \vec{u}, \vec{v}) , we consider the point A of affix $a = -1 - i\sqrt{3}$, the point B of affix $b = -1 + i\sqrt{3}$ and the translation t of vector \overrightarrow{OA}

- 0,5 1) Prove that the affix of the point D image of the point B by the translation t is $d = -2$
2) We consider the rotation R with center D and angle $\left(\frac{2\pi}{3}\right)$.
- 0,5 Show that the affix of the point C image of the point B by the rotation R is $c = -4$
- 0,5 3) a) Write the number $\frac{b-c}{a-c}$ in the trigonometric form
0,5 b) Deduce that $\left(\frac{b-c}{a-c}\right)^2 = \frac{c-d}{b-d}$
- 0,25 4) Let (Γ) be the circle with center D and radius 2, (Γ') the circle with center O and radius 4 and M a point of affix z belonging to the two circles (Γ) and (Γ')
- 0,25 a) Verify that $|z+2|=2$
- 0,5 b) Prove that $z + \bar{z} = -8$ (notice that $|z|=4$)
- 0,25 c) Deduce that the circle (Γ) intersects (Γ') at an unique point which will be determined.

Exercise 3 (3 points) :

An urn contains ten balls: three white balls, three green balls and four red balls indistinguishable by touch. We randomly draw simultaneously three balls from the urn.

0,75 1) Show that $p(A) = \frac{1}{6}$; where A is the event " Not getting any red ball "

0,75 2) Calculate $p(B)$; where B is the event " Getting three white balls or three green balls "

0,75 3) Show that $p(C) = \frac{1}{2}$; where C is the event " Getting exactly one red ball "

0,75 4) Calculate $p(D)$; where D is the event " Getting at least two red balls "

Exercise 4 (2.5 points) :

We consider the function h defined on \mathbb{R} by $h(x) = (x+1)e^x$

0,75 1) a) verify that the function $x \rightarrow xe^x$ is a primitive of h on \mathbb{R} then calculate $I = \int_{-1}^0 h(x) dx$

0,75 b) Using an integration by parts; calculate $J = \int_{-1}^0 (x+1)^2 e^x dx$

0,5 2) a) Solve the differential equation (E): $y'' - 2y' + y = 0$

0,5 b) Show that the function h is the solution of the equation (E) which satisfies the conditions

$$h(0) = 1 \text{ and } h'(0) = 2$$

Problem (8.5 points) :

We consider the numerical function f defined on \mathbb{R} by $f(x) = x(e^{\frac{x}{2}} - 1)^2$.

Let (C) be the curve of f in an orthonormal coordinate system $(O; \vec{i}, \vec{j})$ (unit : 1 cm)

0,5 1) Calculate $\lim_{x \rightarrow +\infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$

0,5 2) Calculate $\lim_{x \rightarrow +\infty} \frac{f(x)}{x}$ and interpret geometrically the result .

0,5 3) a) Show that the line (Δ) with equation $y = x$ is an asymptote to the curve (C) at $-\infty$

0,75 b) Study the sign of $(f(x) - x)$ for all x in \mathbb{R} and deduce the relative position of the curve (C) and the line (Δ)

0,5 4) a) Show that $f'(x) = (e^{\frac{x}{2}} - 1)^2 + xe^{\frac{x}{2}}(e^{\frac{x}{2}} - 1)$ for all x on \mathbb{R}

0,5 b) Verify that $x(e^{\frac{x}{2}} - 1) \geq 0$ for all x in \mathbb{R} then deduce the sign of the derived function f' on \mathbb{R}

0,25 c) Set up the table of variations of the function f in \mathbb{R}

0,5 5) a) Show that $f''(x) = \frac{1}{2}e^{\frac{x}{2}}g(x)$; where $g(x) = (2x+4)e^{\frac{x}{2}} - x - 4$ for all x in \mathbb{R}

0,5 b) From the opposite curve of the function g ,
 Determine the sign of $g(x)$ on \mathbb{R} (Notice : $g(\alpha) = 0$)

0,5 c) Study the concavity of the curve (C) , and determine
 the abscissas of the two inflection points.

1 6) Sketch the curve (C) in the coordinate system $(O; \vec{i}, \vec{j})$
 (We take : $\ln(4) \approx 1,4$, $\alpha \approx -4,5$ and $f(\alpha) \approx -3,5$)

0,5 7) a) Show that the function f admits an inverse function
 f^{-1} defined on \mathbb{R}

0,25 b) Calculate $(f^{-1})'(\ln 4)$

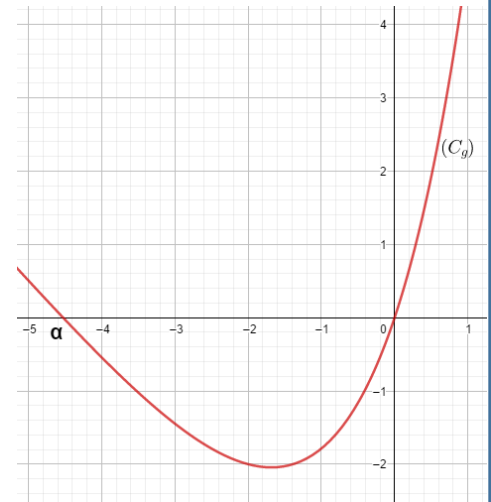
8) Let (u_n) be the numerical sequence defined by $u_0 = 1$ and $u_{n+1} = f(u_n)$ for every n in \mathbb{N}

0,5 a) Show by induction that $0 < u_n < \ln 4$ for every n in \mathbb{N}

0,5 b) Show that the sequence (u_n) is decreasing.

0,25 c) Deduce that the sequence (u_n) is convergent.

0,5 d) Calculate the limit of the sequence (u_n) .



الصفحة : 1 على 3



الامتحان الوطني الموحد للبكالوريا
المسالك الدولية
الدورة العادية 2022

المملكة المغربية
وزارة التربية الوطنية
والتعليم الأولي والابتدائي



المركز الوطني للتقويم والامتحانات

SSSSSSSSSSSSSSSSSSSSSS

**I

- عناصر الإجابة -

NR 22E

7

المعامل

3

مدة
الإنجاز

الرياضيات
مسلك علوم الحياة والأرض ومسلك العلوم الفيزيائية - خيار إنجليزية

المادة
الشعبة والمسلك

On prendra en compte les différentes étapes de la solution et on acceptera toute méthode correcte .

	Questions	Notes	Eléments de réponses
Exercice 1	1-a	0.5	
	1-b	0.25	
	2	0.5	
	3	0.5	0.25 pour la tangence et 0.25 pour le point de tangence
	4-a	0.25	
	4-b	0.5	0.25 pour la tangence et 0.25 pour le point de tangence
	4-c	0.5	0.25 pour le produit scalaire et 0.25 pour la distance
Exercice 2	1	0.5	
	2	0.5	
	3-a	0.5	
	3-b	0.5	
	4-a	0.25	
	4-b	0.5	
	4-c	0.25	
Exercice 3	1	0.75	
	2	0.75	
	3	0.75	
	4	0.75	
Exercice 4	1-a	0.75	
	1-b	0.75	
	2-a	0.5	
	2-b	0.5	

	Questions	Notes	Eléments de réponses
Problème	1	0.5	0.25 pour chaque limite
	2	0.5	0.25 pour la limite et 0.25 pour l'interprétation géométrique
	3-a	0.5	
	3-b	0.75	0.5 pour signe de $(f(x) - x)$ et 0.25 pour la position relative
	4-a	0.5	
	4-b	0.5	0.25 pour la vérification et 0.25 pour le signe de la dérivée
	4-c	0.25	
	5-a	0.5	
	5-b	0.5	
	5-c	0.5	0.25 pour la concavité et 0.25 pour les abscisses des points d'inflexion θ et α
	6	1	Voir le détail dans le graphe ci-dessous
	7-a	0.5	
	7-b	0.25	
	8-a	0.5	
	8-b	0.5	
	8-c	0.25	
8-d	0.5		

